

# Modelling the Variation in Latewood Proportion of Scots Pine Wood from Finland and Sweden

Mika Grekin<sup>1,2</sup>, Erkki Verkasalo<sup>2</sup>



<sup>1</sup> University of Joensuu, Graduate School in Forest Sciences

<sup>2</sup> Finnish Forest Research Institute, Joensuu Research Unit

## Introduction

- Latewood (LW) proportion along with annual ring width explains major part of the variation in wood density
- Basic density affects a variety of physical, mechanical, tooling, etc. properties of wood related to performance in wood processing and end-uses
- LW proportion is highly related to the length of growing period and the rhythm of annual diameter growth
- In this paper, sources of variation in LW proportion of Scots pine (*Pinus sylvestris* L.) wood were analysed with linear mixed models

## Empirical material (Figs. 1&2)

- Sampling was designed to cover the geographic spread and to represent different forest sites and age classes of mature pine stands in Finland and Sweden
- A total of 180 felled sample trees from five regions
- Sample discs from the sections of butt, middle, and top logs
- Two series of measurements along the south-north diagonal were averaged

## Mixed model analysis

- Longitudinal linear model with AR(1) covariance structure
- Only readily available variables on stand and tree characteristics as independents
- Cubic relationship between ring number (cambium age) and LW proportion
- Separate models for the most northerly region and the other four regions
- Due to missing observations data was reduced to a total of 516 positions in 173 trees

$$LW_{xijkl} = \sum_{h=0}^3 (b_h + v_{hkl}) n_{xijkl}^h + b_4 hr_{ijkl} + b_5 SI_{kl} + u_{0jkl} + e_{xijkl}$$

$LW_{xijkl}$  = latewood proportion of ring  $x$  at height position  $i$  in tree  $j$  in stand  $k$  in region  $l$

$n_{xijkl}$  = serial number of ring  $x$  from the pith at height position  $i$  in tree  $j$  in stand  $k$  in region  $l$

$hr_{ijkl}$  = relative height of position  $i$  in tree  $j$  in stand  $k$  in region  $l$

$SI_{kl}$  = site index of stand  $k$  in region  $l$

$b_0 \dots b_5$  = parameters of fixed effects

$u_{0jkl}$  = parameter of tree level random effect;

$u_{0jkl} \sim N(0, \sigma_{tr0}^2)$

$v_{0kl} \dots v_{3kl}$  = parameters of stand level random effect;

$v_{hkl} \sim N(0, \sigma_{stb}^2)$

$e_{xijkl}$  = residual variance;

$e_{xijkl} \sim N(0, \sigma_{e0}^2), Cov(e_{xijkl}, e_{x'ijkl}) = \rho^{|x-x'|} \sigma_{e0}^2$

## Results

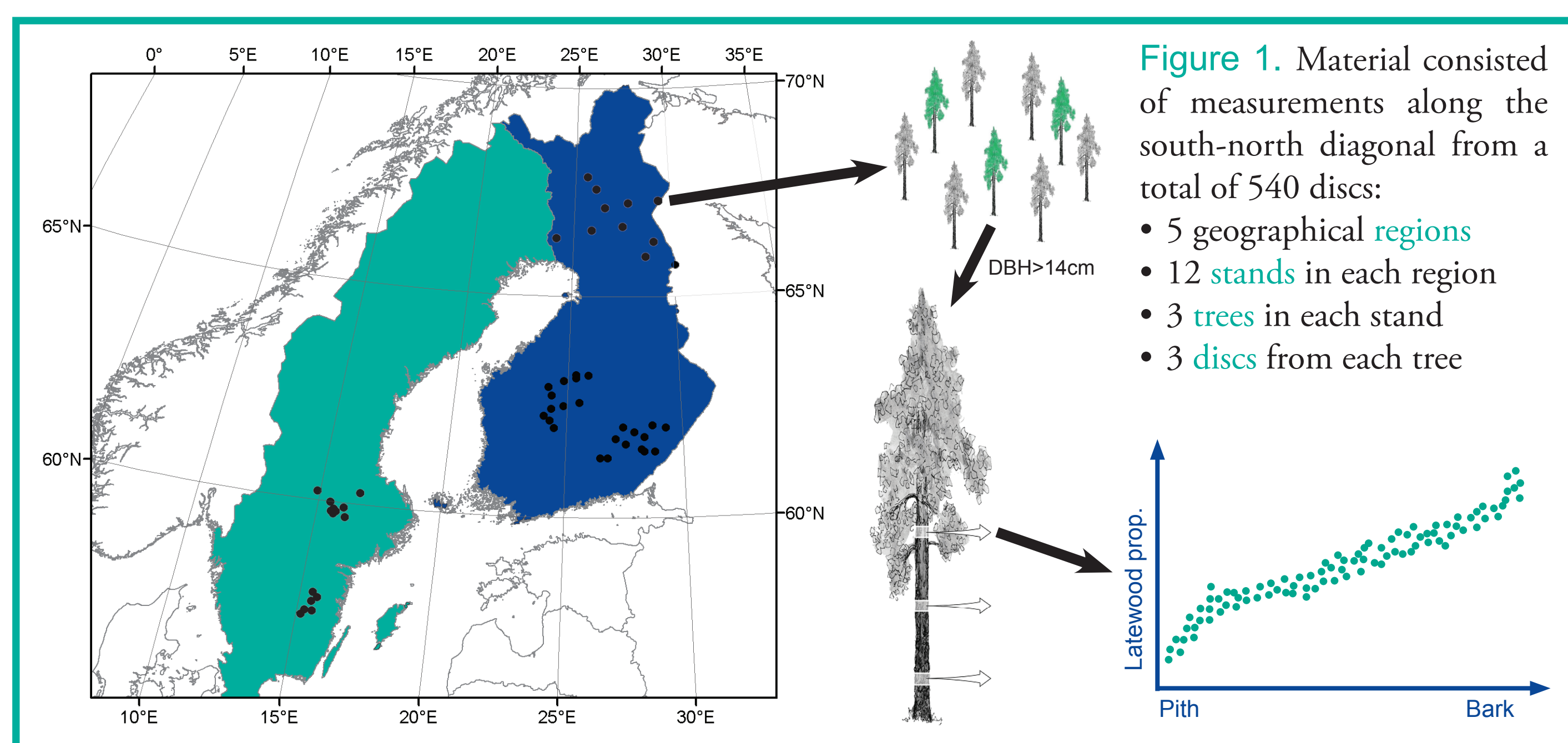
- Highly significant cubic effect of cambium age ( $b_1 \dots b_3$ ) (Table 1)
- Negative effect of relative height position within a tree ( $b_4$ )
- Negative effect of site index ( $b_5$ ), insignificant in northern Finland
- In northern Finland, the average pith-to-bark curves for LW proportion did not differ between stands, contrary to the other four regions ( $\sigma_{st1}^2 \dots \sigma_{st3}^2$ )
- Approx. 20% of the total variation was explained by fixed factors and 50–60% by fixed and random factors both
- Residual accounted for approx. 70–80% of the total random variation

## Conclusions

Latewood proportion

- increased from the pith outward
- decreased from the butt upward
- was the lowest in northern Finland
- decreased toward high site indices in the other four regions

Only one fifth of the total variation could be covered by available background variables



**Table 1.** Estimates of fixed parameters and predicted variance components of the linear mixed models for northern Finland and the other four regions.

	Fixed parameters					
	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$
NF	23.6 *	1.45 **	-0.0764 **	.0023 *	-7.41 **	-.349
Others	25.0 *	7.34 **	-1.23 **	.0728 **	-11.9 **	-5.42 **

### Variance components

	$\sigma_{tr0}^2$	$\sigma_{st0}^2$	$\sigma_{st1}^2$	$\sigma_{st2}^2$	$\sigma_{st3}^2$	$\sigma_{e0}^2$	$\rho$
NF	7.26 *	3.93	.110	.0001	.0000	26.4 **	.383 **
Others	5.76 **	.0000	6.04 **	.308 **	.001 **	22.7 **	.299 **

\* Significant at the 0.01 level, \*\* Significant at the 0.001 level

**Figure 2.** Basic characteristics (min–average–max) of stands (left) and sample trees (right) in different regions.

